

Contributions to Sliced Inverse Regression

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Abstract: This report summarizes my contributions towards the improvement of the Sliced Inverse Regression method.

Sliced Inverse Regression (SIR) is an effective method for dimension reduction in high-dimensional regression problems. It has been successfully applied to estimation of reference curves [1, 2].

The original method, however, requires the inversion of the predictors covariance matrix. In case of collinearity between these predictors or small sample sizes compared to the dimension, the inversion is not possible and a regularization technique has to be used. The proposed approach is based on a Fisher Lecture given by R.D. Cook where it is shown that SIR axes can be interpreted as solutions of an inverse regression problem. A Gaussian prior is introduced on the distribution on the unknown parameters of the inverse regression problem in order to regularize their estimation [3]. I showed that some existing SIR regularizations can enter this framework, which permits a global understanding of these methods [4]. Three new priors are proposed leading to new regularizations of the SIR method. A comparison on simulated data as well as an application to the estimation of Mars surface physical properties from hyperspectral images are provided [5, 6, 7].

A sequential extension of SIR dedicated to very large datasets [8] was also developed as well as an extension to multivariate outputs [9]. I also worked on the adaptation of SIR to non-Gaussian datasets [10, 11] via mixtures and heavy-tailed distributions.

References

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